

Problem Set 3.7

1. Find $y' = \frac{dy}{dx} = D_x(y)$ by implicit differentiation.

(1) $xy + 2x + 3y^2 = 4$

(2) $\sin(xy) = y^2$

2. (1) Find y' and y'' at (1,1) if $x^2 + xy + y^2 = 3$

(2) Find the equation of the tangent line to the curve $x^2 + xy + y^2 = 3$ at (1,1).

Problem Set 3.10

Derivatives

| | |
|--|-------------------------------------|
| $D_x(\sin^{-1}x) = \frac{1}{\sqrt{1-x^2}}$ | $D_x(\tan^{-1}x) = \frac{1}{1+x^2}$ |
| $D_x(\sinh x) = \cosh x$ | $D_x(\cosh x) = \sinh x$ |

3. Find the derivative of the function.

(1) $y = \sin^{-1}(2x + 1)$

(2) $y = \ln(\tan^{-1}x)$

(3) $y = \sinh x \cosh 3x$

Problem Set 3.11

Let $y = f(x)$ and x change from a to $a + \Delta x$

actual change : $\Delta y = f(a + \Delta x) - f(a)$

differential : $dy = f'(a)dx = f'(a)\Delta x$

4. Find Δy and dy where $y = 2x - x^2$; $x = 2$,
 $\Delta x = dx = -0.3$

At $x = a$,

linear approximation : $L(x) = f(a) + f'(a)(x - a)$

5. Find the linear approximation to the function

$f(x) = \sin x$ at $x = \frac{\pi}{6}$.

Approximation $f(a + \Delta x)$ where $\Delta x = dx$ using;

a differential : $f(a + \Delta x) \approx f(a) + f'(a)dx$

a linear approximation : $f(a + \Delta x) \approx L(a + \Delta x)$

6. Approximate $\sqrt{99.8}$.

(1) Find $f(x)$ and a point a near 99.8 to approximate $\sqrt{99.8}$.

$f(x) =$

$a =$

(2-1) [method1] Use a differential to approximate $\sqrt{99.8}$.

(2-2) [method2] Use a linear approximation to approximate $\sqrt{99.8}$.